

**Weekly Review #1**

**Name:** \_\_\_\_\_

**SHOW ALL WORK**

1. Given  $p = x - \frac{\sqrt{y}}{z}$ ,  $x = 1.775$ ,  $y = 1.44$  and  $z = 48$ ,

- (a) calculate the value of  $p$ .

(2)

Barry **first** writes  $x$ ,  $y$  and  $z$  correct to one significant figure and **then** uses these values to estimate the value of  $p$ .

- (b) (i) Write down  $x$ ,  $y$  and  $z$  each correct to one significant figure.

- (ii) Write down Barry's estimate of the value of  $p$ .

(2)

- (c) Calculate the percentage error in Barry's estimate of the value of  $p$ .

(2)

**(Total 6 marks)**

2. (a) List the elements of the set  $A = \{x \mid -4 \leq x \leq 2, x \text{ is an integer}\}$ . (1)

A number is chosen at random from set  $A$ .

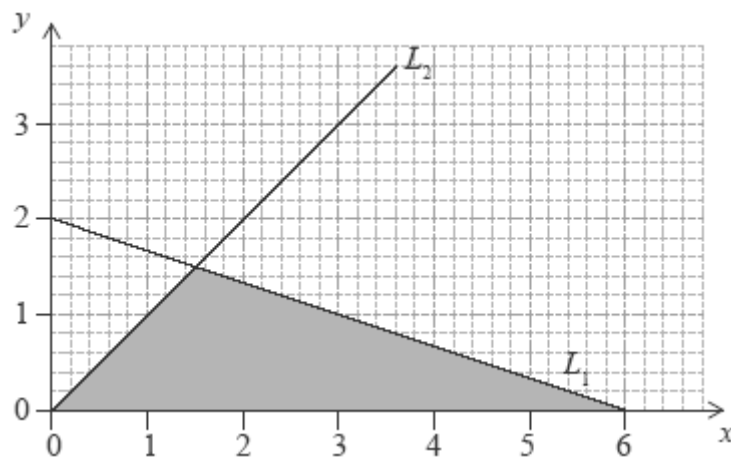
Write down the probability that the number chosen is

- (b) a negative integer; (2)

- (c) a positive even integer; (1)

- (d) an odd integer less than  $-1$ . (2)
- (Total 6 marks)

3. The diagram shows the straight lines  $L_1$  and  $L_2$ . The equation of  $L_2$  is  $y = x$ .



- (a) Find (3)
- (i) the gradient of  $L_1$ ;
- (ii) the equation of  $L_1$ .

- (b) Find the area of the shaded triangle. (3)
- (Total 6 marks)

4. The equation of the line  $R_1$  is  $2x + y - 8 = 0$ . The line  $R_2$  is perpendicular to  $R_1$ .

(a) Calculate the gradient of  $R_2$ .

(2)

The point of intersection of  $R_1$  and  $R_2$  is  $(4, k)$ .

(b) Find

(i) the value of  $k$ ;

(ii) the equation of  $R_2$ .

(4)

(Total 6 marks)

5. The seventh term,  $u_7$ , of a geometric sequence is 108. The eighth term,  $u_8$ , of the sequence is 36.

(a) Write down the common ratio of the sequence.

(1)

(b) Find  $u_1$ .

(2)

The sum of the first  $k$  terms in the sequence is 118 096.

(c) Find the value of  $k$ .

(3)

(Total 6 marks)

6.  $U$  is the set of all the **positive** integers less than or equal to 12.  
 $A$ ,  $B$  and  $C$  are subsets of  $U$ .

$$A = \{1, 2, 3, 4, 6, 12\}$$

$$B = \{\text{odd integers}\}$$

$$C = \{5, 6, 8\}$$

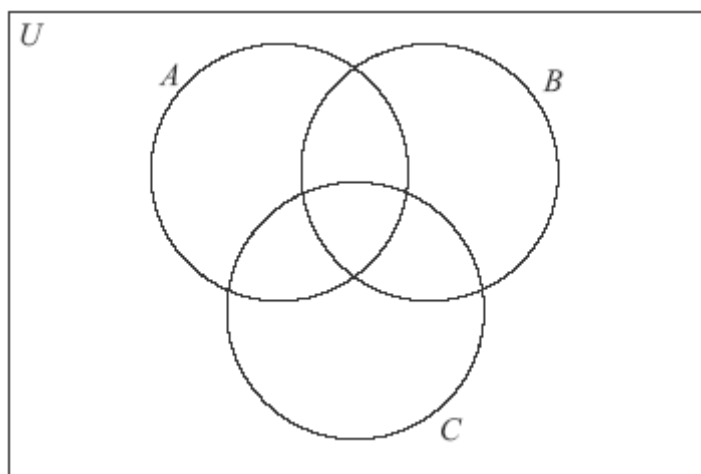
- (a) Write down the number of elements in  $A \cap C$ .

(1)

- (b) List the elements of  $B$ .

(1)

- (c) Complete the following Venn diagram with **all** the elements of  $U$ .



(4)

(Total 6 marks)

7. 10 000 people attended a sports match. Let  $x$  be the number of adults attending the sports match and  $y$  be the number of children attending the sports match.

(a) Write down an equation in  $x$  and  $y$ .

(1)

The cost of an adult ticket was 12 AUD. The cost of a child ticket was 5 AUD.

(b) Find the total cost for a family of 2 adults and 3 children.

(2)

The total cost of tickets sold for the sports match was 108 800 AUD.

(c) Write down a second equation in  $x$  and  $y$ .

(1)

(d) Write down the value of  $x$  and the value of  $y$ .

(2)

(Total 6 marks)

8. A manufacturer in England makes 16 000 garden statues. 12 % are defective and cannot be sold.

- (a) Find the number of statues that are non-defective.

(2)

The manufacturer sells each non-defective statue for 5.25 British pounds (GBP) to an American company. The exchange rate from GBP to US dollars (USD) is 1 GBP = 1.6407 USD.

- (b) Calculate the amount in USD paid by the American company for all the non-defective statues. Give your answer correct to **two decimal places**.

(2)

The American company sells one of the statues to an Australian customer for 12 USD. The exchange rate from Australian dollars (AUD) to USD is 1 AUD = 0.8739 USD.

- (c) Calculate the amount that the Australian customer pays, in AUD, for this statue. Give your answer correct to **two decimal places**.

(2)

**(Total 6 marks)**

9. Shiyun bought a car in 1999. The value of the car  $V$ , in USD, is depreciating according to the exponential model

$$V = 25\,000 \times 1.5^{-0.2t}, t \geq 0,$$

where  $t$  is the time, in years, that Shiyun has owned the car.

- (a) Write down the value of the car when Shiyun bought it.

(1)

- (b) Calculate the value of the car three years after Shiyun bought it. Give your answer correct to **two decimal places**.

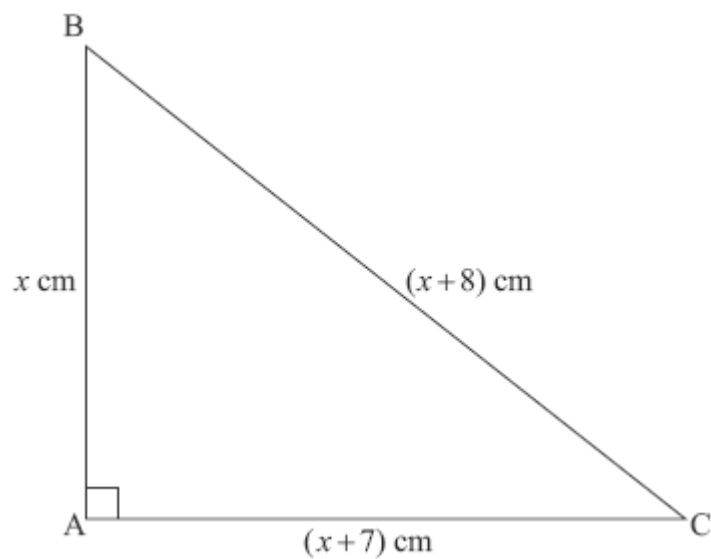
(2)

- (c) Calculate the time for the car to depreciate to half of its value since Shiyun bought it.

(3)

**(Total 6 marks)**

10. In the diagram,  $\hat{BAC} = 90^\circ$ . The length of the three sides are  $x$  cm,  $(x + 7)$  cm and  $(x + 8)$  cm.



*diagram not to scale*

- (a) Write down and **simplify** a quadratic equation in  $x$  that links the three sides of the triangle. (3)
- (b) Solve the quadratic equation found in part (a). (2)
- (c) Write down the value of the perimeter of the triangle. (1)

(Total 6 marks)